### Gene trees vs species tree

Tomáš Fér 2025

some parts based on

<u>http://tandy.cs.illinois.edu/astral-tutorial.pdf</u> (Siavash Mirarab)
<u>http://tandy.cs.illinois.edu/astrid-ssb-v2.pdf</u> (Pranjal Vachaspati)

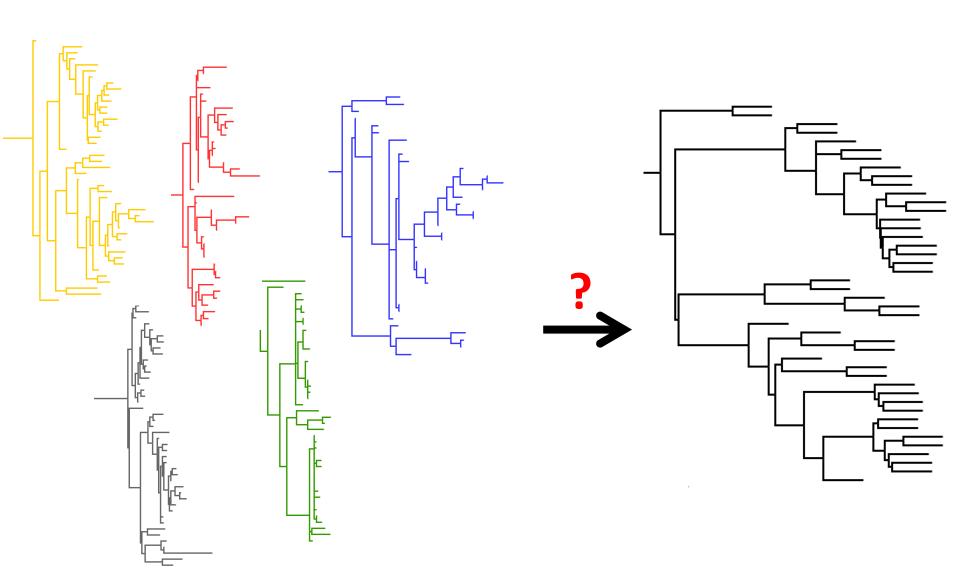
### Outline

- gene trees and gene tree-species tree incongruence
- species tree estimation approaches
- multispecies coalescence (MSC)
  - coestimation (\*BEAST)
  - summary methods
- ASTRAL
  - quartets under MSC
  - input/output
  - assumptions/problems
  - multiple individuals per species
  - filtering data
  - localPP vs. MLBS
  - branch lengths
  - tree scoring
  - polytomy testing
- ASTRID
  - principle, accuracy
- MRI
- Quartet Sampling
  - principle, applications
- Gene selection/filtering
  - calculating alignment/tree characteristics

### **Practicals**

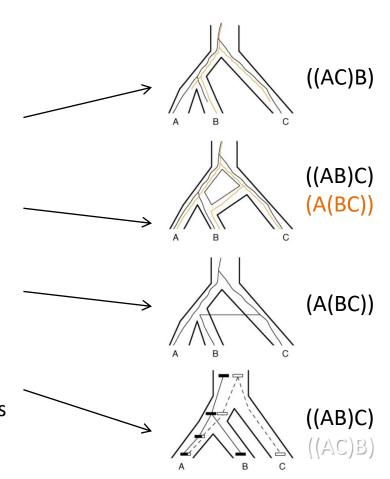
- ASTRAL
- ASTRID
- MRL
- Quartet Sampling
- alignment/tree characteristics (AMAS/R)

### Species tree from gene trees

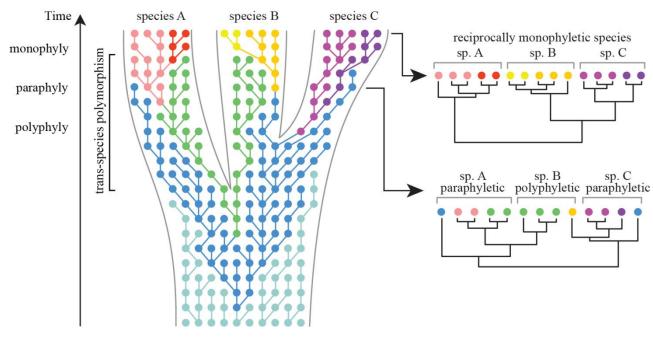


### Gene tree incogruence

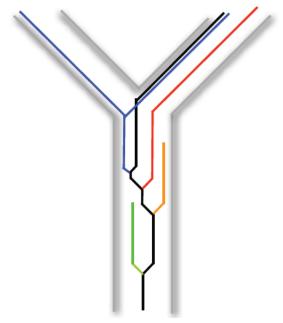
- incomplete lineage sorting (ILS)/deep coalescence
- gene duplications and losses (GDL)
  - orthology problem
- hybridization/(allo)polyploidization
  - affects whole genomes
- horizontal gene transfer (HGT)
  - affects small DNA segments
- recombination
  - different histories for neighboring segments in genes



### Coalescence processes

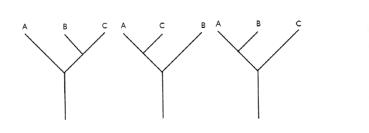


https://frederikleliaert.wordpress.com/green-algae/dna-based-species-delimitation-in-algae/



incomplete lineage sorting

### Species tree estimation



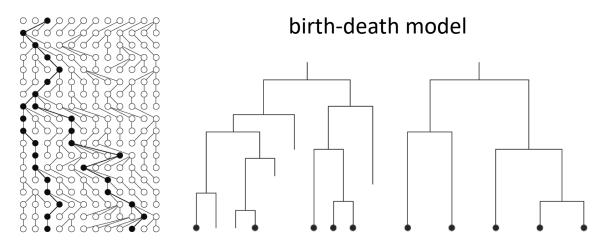
- concatenation
- multispecies coalescence
  - \*BEAST (coestimation of gene trees and species tree)
  - summary methods (combining gene trees)
- supertree methods
  - MRL (maximum representation using likelihood)
- Bayesian concordance analysis (BUCKy)
  - quartet-based Bayesian species tree estimation
- site-based methods
  - SNAPP, SVDquartets

### Concatenation

- put all the loci after each other (superalignment, supermatrix)
- very good accuracy under low ILS model conditions
- i.e., good approach unless strong ILS
- single partition model
  - the whole alignment analyzed with the same parameters
  - statistically inconsistent
- multiple partitions model (ML or Bayesian)
  - each alignment (or even codon position) analyzed with separate parameters
  - best partitioning scheme by, e.g., PartitionFinder or ModeltestNG or IQtree
  - fully partitioned analysis
  - maximum likelihood (CA-ML) RAxML-ng, ExaML
  - or Bayesian inference MrBayes, ExaBayes

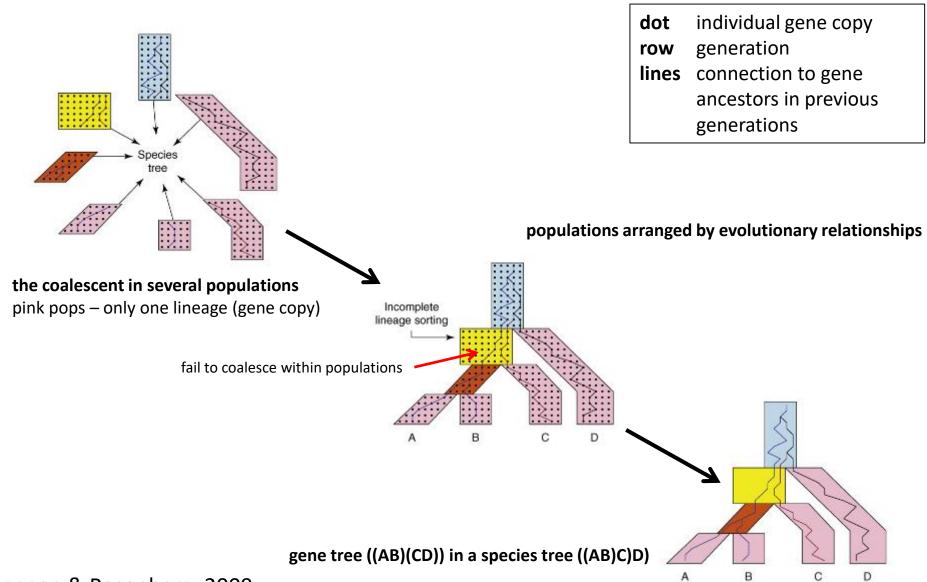
- coalescent model applied to gene trees in a species tree
  - combines coalescent and birth-death models

### coalescence

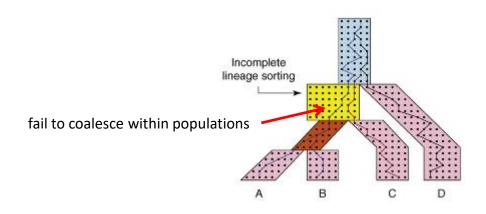


- used to assemble separate coalescent processes occurring in populations connected by an evolutionary tree
  - coalescent tree distribution (probability of sharing common ancestor t generations back)
  - birth-death model with stochastic rate of birth and death
  - describes probability of gene tree(s) within a species tree

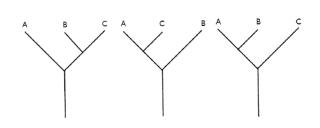
### coalescence birth-death model

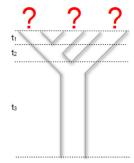


- (incomplete) lineage sorting
  - particular types of genealogical pattern
  - process explaining gene tree discordance
  - failure of lineages in a population to coalesce



### Species tree estimation



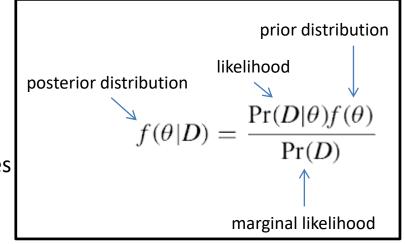


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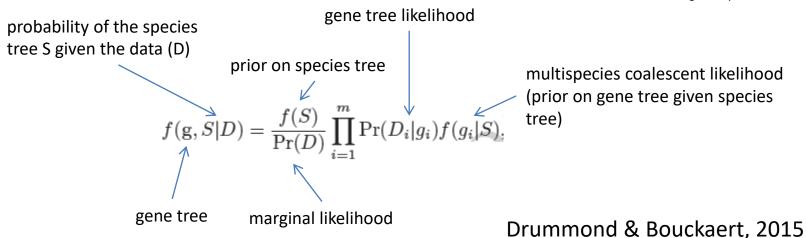
### \*BEAST

### STAR-BEAST = **S**pecies **T**ree **A**ncestral **R**econstruction

- Bayesian framework for species tree reconstruction
- assumptions
  - no recombination within locus
  - free recombination between loci
  - no hybridization
  - each sample mapped to appropriate species



original Bayesian theorem



### \*BEAST

### STAR-BEAST = Species Tree Ancestral Reconstruction

- co-estimates gene trees and species tree
- most accurate species tree method
- computationally intensive
- not suitable for large datasets, i.e.
  - no more than ~50 loci
  - no more than ~20-30 species

 BBCA – divide-and-conquer technique (Zimmermann et al., 2014)

### Summary methods

### Species tree estimation

### require rooted gene trees

- MP-EST maximum pseudo-likelihood approach for estimating species trees
- STAR species tree estimation using average ranks of coalescences

### unrooted gene trees

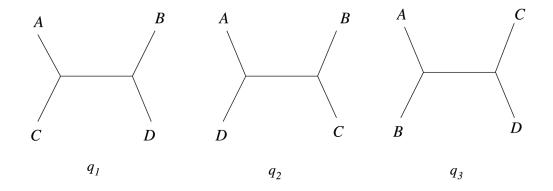
- STEAC species tree estimation using average coalescence times
- ASTRAL Accurate Species Tree Reconstruction ALgorithm
- ASTRID Accurate Species TRees from Internode Distances (reimplementation of NJ<sub>st</sub> method)

**site-based methods** (estimate species trees from the distribution on site pattern within unlinked loci)

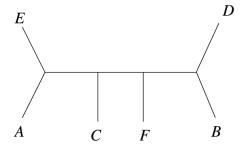
- SNAPP SNP and AFLP Package for Phylogenetic analysis
- SVDquartets

### Tree reconstruction from quartets

- quartet unrooted tree over 4 taxa
- three possible quartets
- only one quartet q is consistent with final tree T



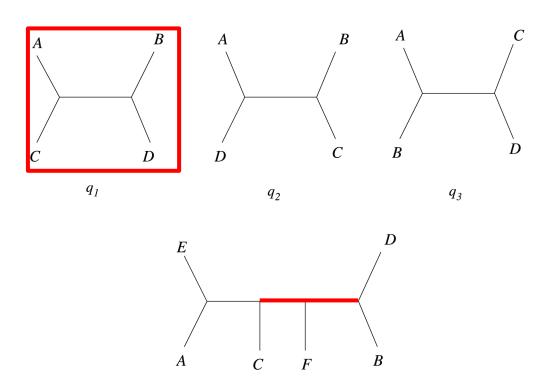
 which quartet is consistent with T?



7

### Tree reconstruction from quartets

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- only one quartet q is consistent with final tree T



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### **ASTRAL**

### Accurate Species Tree Reconstruction Algorithm https://github.com/smirarab/ASTRAL

- unrooted gene trees
- species tree that agrees with the largest number of quartet trees induced by the set of gene trees
- weighting all three alternative quartet topologies according to their relative frequencies within gene trees
  - much more frequent topology trees without this topology are penalized
  - similar frequencies (i.e., close to 0.33) the quartet has little impact to optimization
- final species tree with
  - local posterior probability that the branch is in the species tree
  - the length of internal branches in coalescent units

### Unrooted quartets under MSC model

- **for a quartet (4 species)** the most probable unrooted quartet tree (among the gene trees) is the unrooted species tree topology
- **for 5 or more species** the unrooted species tree topology can be different from the most probable gene tree (called "anomaly zone")
  - break gene trees into quartets of species
  - find the species tree with the maximum number of induced quartet trees shared with the collection of input gene trees (NP-hard optimization problem)
  - statistically consistent under the multispecies coalescent model with errorfree input
  - solved by dynamic programming ASTRAL

### **ASTRAL** versions

- ASTRAL-I (<v. 4.3.7)</li>
- ASTRAL-II (<v. 5.1.0)</li>
  - improved the accuracy at the expense of running time
  - can handle polytomies
- ASTRAL-III (>v. 5.1.1)
  - changed the search space again for a better running time versus accuracy trade-off
  - improved running time for unresolved trees
- ASTRAL-IV (within ASTER)
  - scalable alternative
  - computes terminal and internal branch length in substitution-per-site units

### ASTRAL input/output

- input unrooted gene trees
  - missing data allowed
  - polytomies allowed
  - multiple alleles per species allowed

- output estimated unrooted species tree
  - branch lengths in coalescent units (on internal branches)
  - measure of branch support (LPP, local posterior probability)

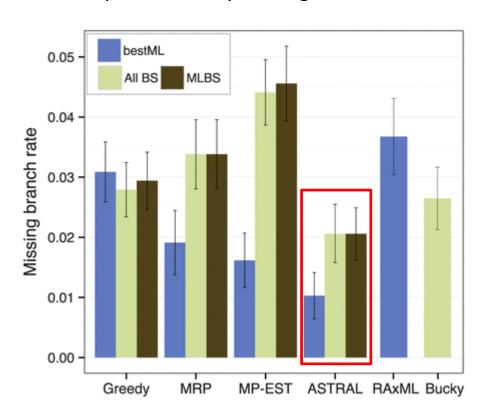
### ASTRAL problems

- assumption for statistical consistency
  - randomly distributed sample of gene trees
    - recombination-free
    - reticulation-free
    - error-free
    - orthologous

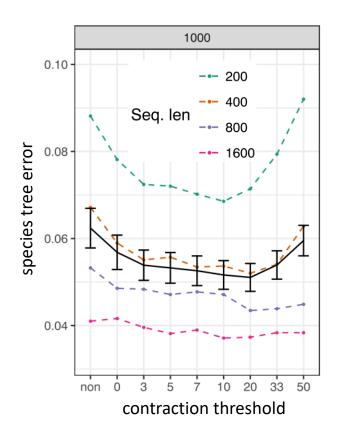
• in practice: reduced accuracy with low accuracy gene trees

### How input gene trees influence ASTRAL

BS and MLBS degrade accuracy compared to simple ML gene trees



contraction of branches with very low support helps

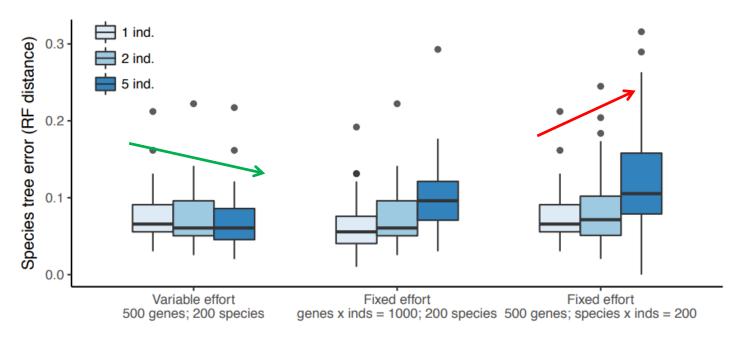


Mirarab et al. 2014, Bioinformatics

Zhang et al. 2018, BMC Bioinformatics

### Multiple individuals per species

- sampling multiple individuals extra signal
- individual can be non-monophyletic in gene trees (i.e., in recently diversified groups)



only helpful with variable (i.e., increased) sequencing effort, not with fixed (i.e., when 'nr. genes × nr. individuals' remains the same)

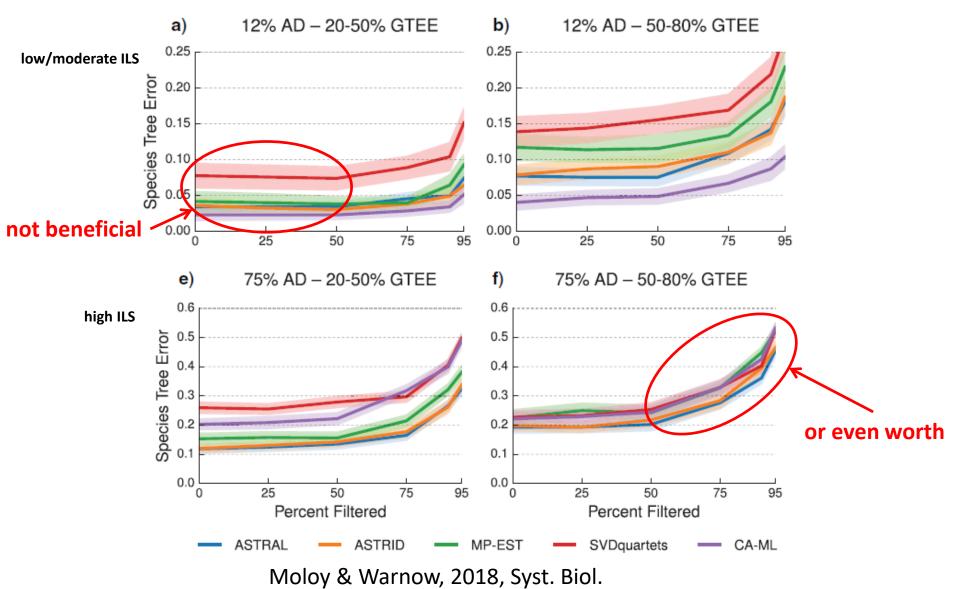
### Filtering?

- genes based on missing species?
  - generally not beneficial (Moloy & Warnow 2018)

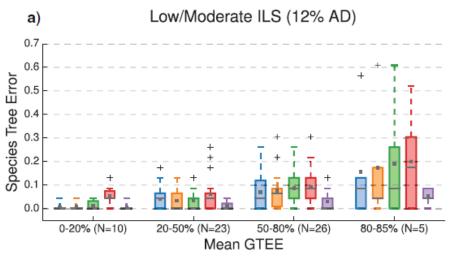
- genes based on gene tree estimation error (GTEE)
  - depends on condition (Moloy & Warnow 2018)

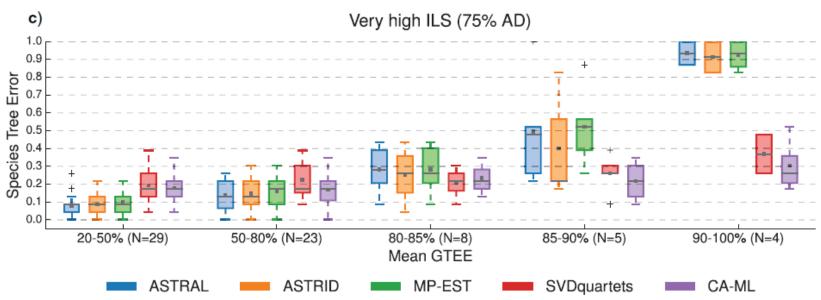
- filtering fragmentary sequences (and keeping gene)
  - often beneficial (Sayyari, Whitfield, Mirarab, 2017)

### Gene filtering – missing species



### Gene filtering – gene tree estimation error





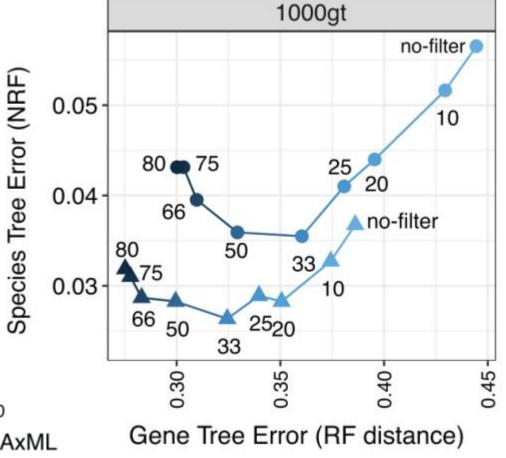
Moloy & Warnow, 2018, Syst. Biol.

### Filtering fragmentary sequences

remove fragmentary data from genes

BUT keep genes

often beneficial



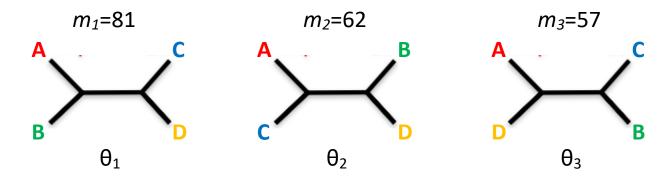
0.6 0.7 0.8 0.9 1.0 ■ FastTre ▲ RAxML

Occupancy

http://tandy.cs.illinois.edu/astral-apro.pdf

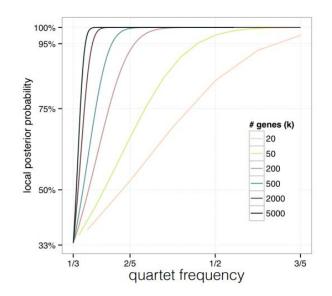
### Local posterior probability

quartet frequencies follow a multinomial distribution



- P (gene tree seen  $m_1/m$  times = species tree) =  $P(\theta_1 > 1/3)$ 
  - possible to solve analytically
  - resulting measure is localPP
  - for *n*>4 averaging quartet scores
- more accurate and faster than multi-locus bootstrap (MLBS; Seo 2008)

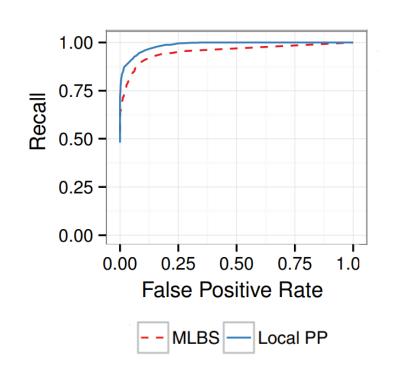
increased number of genes = increased support decreased discordance = increased support



### localPP vs. MLBS

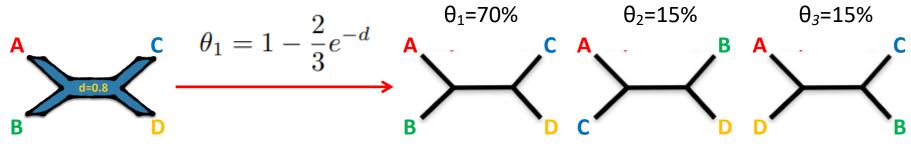
- LPP = local posterior probability
- MLBS = multi-locus bootstrap (Seo, 2008)
  - requires bootstrap replicate trees for each gene

- localPP is more accurate than bootstrapping
- calculating localPP is also ca. 100× faster



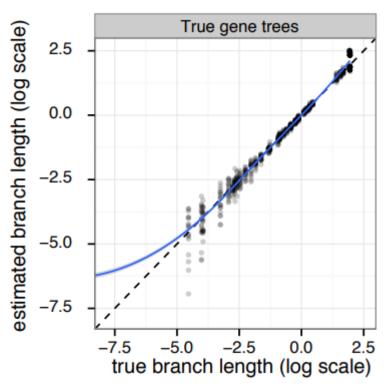
### Branch length of ASTRAL trees

- branch length in coalescence units = the level of discordance
- for a single quartet (i.e., n=4) reverse the discordance formula to get multilocus estimate
- for n>4 average frequencies around the branch

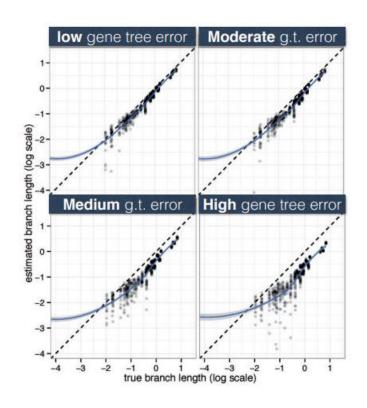


http://tandy.cs.illinois.edu/astral-apro.pd

### Branch lengths (BL) accurracy



correct BL estimate with true gene trees



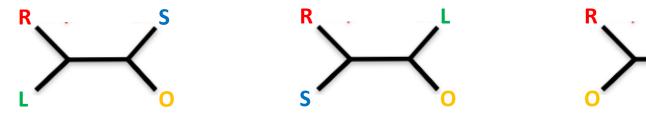
underestimated BL estimate with errorprone gene trees

### ASTRAL problems

- assumption for statistical consistency
  - randomly distributed sample of gene trees
    - recombination-free
    - reticulation-free
    - error-free
    - orthologous
- in practice: reduced accuracy with low accuracy gene trees
- branch length
  - only for internal branches (unless multiple individuals per species)
  - in coalescent units, i.e., "true value" is a function of population size and generation time
- local posterior probability (LPP)
  - better than MLBS (empirically) but based on many assumptions

### **ASTRAL** tree scoring

- quartet support (-t 1) percentage of quartets that agrees with the branch (measuring the amount of gene tree conflict)
- alternative posteriors (-t 4) three localPP: (1) main topology (RL|SO), (2) first alternative (RS|LO), (3) second alternative (RO|LS)



- full annotation (-t 2)
- alternative quartet topologies (-t 8) quartet support for the main and alternative topologies
- polytomy test (-t 10) runs a test if the hypothesis (branch is a polytomy) could be rejected

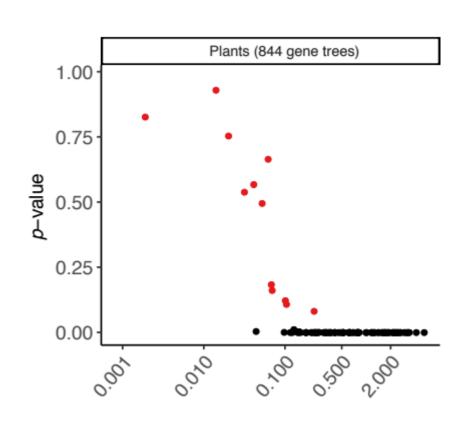
### Hard polytomy test

- soft polytomy unresolved relationships in an estimated tree
- hard polytomy multifurcation in the true tree
- null hypothesis branch has zero length and should be removed to create a polytomy
- try to reject null hypothesis
  - reject (i.e., p<0.05) branch does exist (is supported by the data)</li>
  - fail to reject branch can be replaced by polytomy
- in ASTRAL with '-t 10'
- Sayyari, Erfan, Mirarab (2018): Testing for polytomies in phylogenetic species trees using quartet frequencies. Genes 9: 132

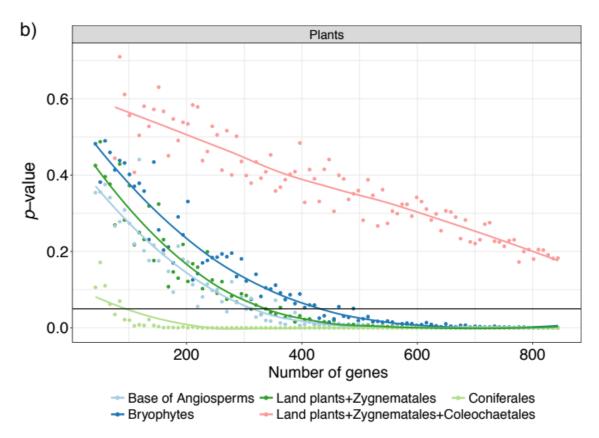
### Polytomy vs. branch length

- x-axis branch length in log CU (coalescence units)
- y-axis polytomy test p-value
- points with p < 0.05 in black</li>

 longer branches are usually supported



# Polytomy tests – plant dataset



- polytomy hypotheses rejected with increasing number of genes
- correct relationship between Chara and Coleochaetales remains hard to resolve, may be with more data?

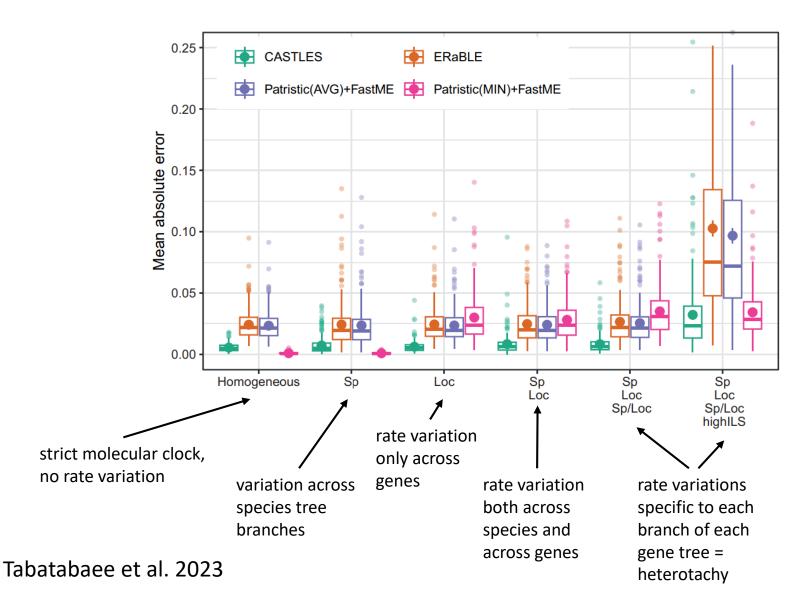
Sayyari, Erfan, Mirarab, 2018, Genes

#### **ASTRAL-IV**

https://github.com/chaoszhang/ASTER/blob/master/tutorial/astral4.md

- scalable alternative to ASTRAL large datasets, multiindividual, gene trees with missing taxa
- integrates CASTLES-II algorithm (Tabatabaee et al. 2023) computes terminal and internal branch lengths in expected substitution-per-site units
  - Coalescent-Aware Species Tree Length Estimation in Substitution-unit
  - addresses gene tree heterogeneity due to incomplete lineage sorting (ILS), as modeled by the multi-species coalescent (MSC) model
  - does not assume strict molecular clock
  - superior accuracy compared to alternatives
- part of ASTER\* (<a href="https://github.com/chaoszhang/ASTER">https://github.com/chaoszhang/ASTER</a>) –
   Accurate Species Tree EstimatoR

# Accuracy of CASTEL algorithm



## **ASTRAL** practical

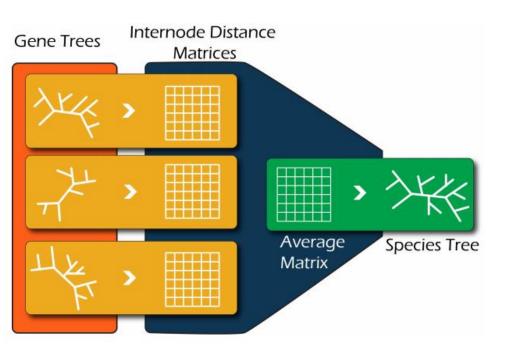
#### https://github.com/smirarab/ASTRAL

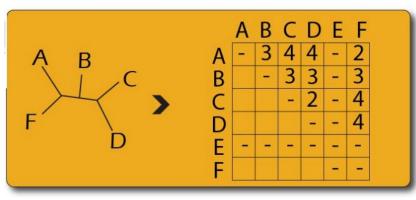
- help: java -jar astral.5.7.3.jar
- **simple run**: java -jar astral.5.7.3.jar -i input.trees -o output.tre
- scoring existing tree: java -jar astral.5.7.3.jar -q existing.tre -i input.trees -o output.tre
- **branch annotation**: java -jar astral.5.7.3.jar -q existing.tre -i input.trees -t 2 -o output.tre
- polytomy test: java -jar astral.5.7.3.jar -q existing.tre -i input.trees -t 10 -o output.tre
- multilocus bootstrapping: java -jar astral.5.7.3.jar -i input.trees -b bootstrapTreeList -o output.tre (bootstrapTreeList is a text file containing file path of gene tree bootstrap files, one per line, i.e., file full of paths of files full of trees)

#### **ASTRID**

# Accurate Species TRees from Internode Distances github.com/pranjalv123/ASTRID

- species tree computed from internode distance matrices
- reimplementation of NJst method (Liu & Yu, 2011)
- uses FastME-2 (Lefort, Desper & Gascuel 2015)
- fast, can scale to extremely large datasets





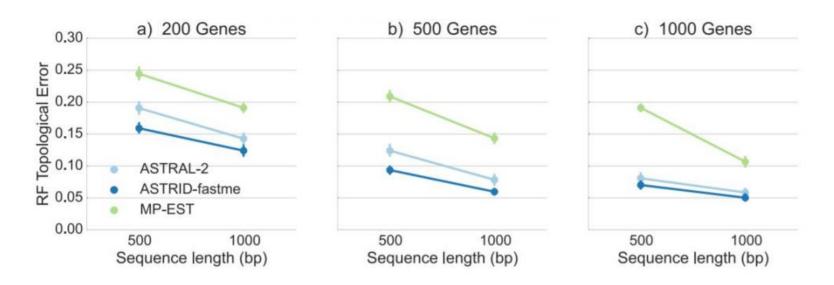
Pranjal Vachaspati

http://tandy.cs.illinois.edu/astrid-ssb-v2.pdf

# http://tandy.cs.illinois.edu/astrid-ssb-v2.pdf

# **ASTRID** accuracy

high accuracy on datasets with ILS



47-taxon simulated dataset, high ILS

# **ASTRID** practical

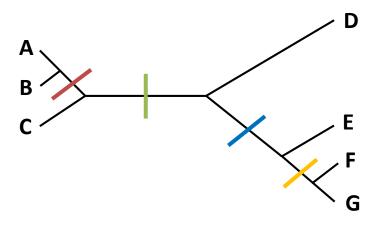
- download ASTRID binary
  - https://github.com/pranjalv123/ASTRID/releases
  - Win version: <a href="https://github.com/pranjalv123/ASTRID-1/releases">https://github.com/pranjalv123/ASTRID-1/releases</a>
- run over your trees
  - ASTRID -i input.trees -o output.tre
- no support values unless you do MLBS
  - ASTRID -i input.trees -b bootstrapTreeList -o output.tre

#### **MRL**

Maximum Representation with Likelihood; Nguyen et al. 2012

- supertree method estimates species tree on full taxon sets from sets of smaller trees (i.e., with missing species)
- encodes a set of gene trees by a large randomized matrix
  - using mrp.jar; https://github.com/smirarab/mrpmatrix
- each edge (branch) in each gene tree
  - '0' for the taxa that are on one side of the edge
  - '1' for the taxa on the other side
  - '?' for all the remaining taxa (i.e., the ones that do not appear in the tree)
- MRL matrix is analyzed using heuristics for a symmetric 2state Maximum Likelihood
  - in RAxML as 'BINCAT' model

# MRL binary matrix



randomization

	*	*	*	*	•••
A	0	1	1	0	
В	0	1	1	0	
C	1	1	1	0	
D	1	0	1	0	
E	1	0	0	0	
F	1	0	0	1	
G	1	0	0	1	
IJ	2	2	2	2	

#### **MRL**

Maximum Representation with Likelihood; Nguyen et al. 2012

- download mrp.jar from <a href="https://github.com/smirarab/mrpmatrix">https://github.com/smirarab/mrpmatrix</a>
- run on your trees
  - java -jar mrp.jar trees.nwk MRLmatrix.phylip -randomize
- analyze MRL matrix is using RAxML as 'BINGAMMA' model
  - raxmlHPC-PTHREADS -T nrCores -f a -s MRLmatrix.phylip -n MRLresult -m BINGAMMA -p 1234 -x 1234 -N nrBSreps

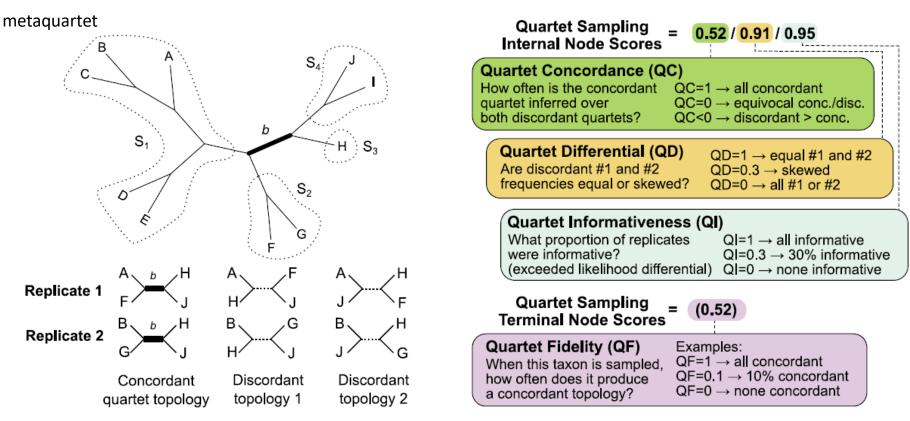
## Quartet Sampling (QS)

Replacement for bootstrap in phylogenomic studies...

- quartet-based evaluation system
- synthetizes several phylogenetic and genomic analytical approaches
- discordance testing
- distinguishes strong conflict from weak support
- three different scores per branch
  - Quartet Concordance (QC)
  - Quartet Differential (QD)
  - Quartet Informativeness (QI)
- terminal node score
  - Quartet Fidelity (QF)

Pease et al. (2018): Quartet Sampling distinguishes lack of support from conflicting support in the green plant tree of life. *American Journal of Botany* 105(3): 385–403.

- takes an existing phylogenetic topology and a molecular dataset
- evaluates internal branches likelihood for all three possible phylogenies for the randomly selected quartets spanning particular branch



Pease et al. (2018): Quartet Sampling distinguishes lack of support from conflicting support in the green plant tree of life. *American Journal of Botany* 105(3): 385–403.

#### Replacement for bootstrap in phylogenomic studies...

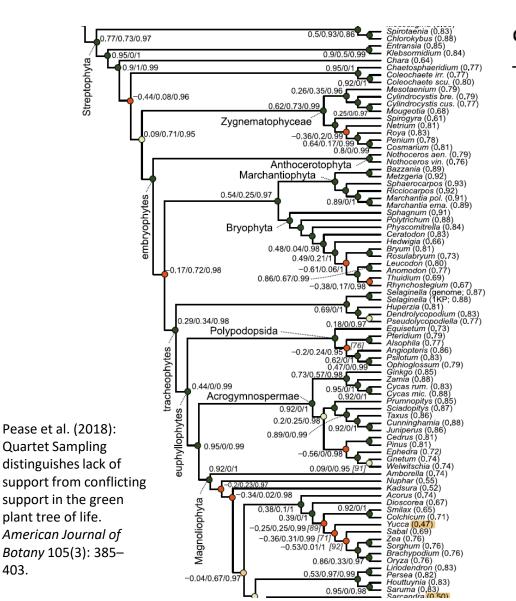
TABLE 1. Quartet Sampling (QS) score interpretation.

Example QS score (QC/QD/QI)	Interpretation
1.0/-/1.0	Full support: All sampled quartet replicates support the focal branch ( $QC = 1$ ) with all trees informative when likelihood
	cutoffs are used $(QI = 1)$ .
0.5/0.98/0.97	Strong support: A strong majority of quartets support the focal branch (QC = 0.5), and the low skew in discordant
	frequencies (QD $\approx$ 1) indicate no alternative history is favored.
0.7/0.1/0.97	Strong support with discordant skew A strong majority of quartets support the focal branch (QC = 0.7), but the skew in
	discordance (QD = 0.1) indicates the possible presence of a supported secondary evolutionary history.
0.05/0.96/0.97	Weak support: Only a weak majority of quartets support the focal branch (QC = 0.05), and the frequency of all three
	possible topologies is similar (QD $\approx$ 1).
0.1/0.1/0.97	Weak support with discordant skew: Only a weak majority of quartets support the focal branch (QC = 0.1), and the skew in
	discordance ( $QD = 0.1$ ) indicates the possible presence of a supported secondary evolutionary history.
-0.5/0.1/0.93	Counter-support: A strong majority of quartets support one of the alternative discordant quartet arrangement history
	(QC < 0; QD expected to be low).
1/0.97/0.05	Poorly informed Despite supportive QC/QD values, only 5% of quartets passed the likelihood cutoff (QI = 0.05), likely
	indicating few informative sites.
0.0/0.0/1.0	Perfectly conflicted: The (unlikely) case where the frequencies of all three possible trees are equal and all trees are
	informative, which indicates a rapid radiation or highly complex conflict.

Notes: QC = Quartet Concordance; QD = Quartet Differential; QI = Quartet Informativeness.

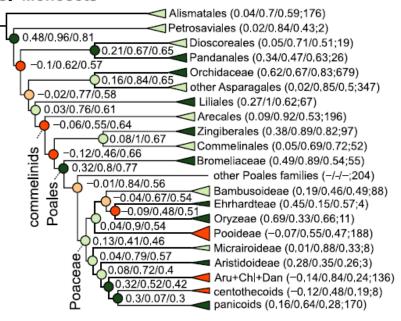
Pease et al. (2018): Quartet Sampling distinguishes lack of support from conflicting support in the green plant tree of life. *American Journal of Botany* 105(3): 385–403.

# Quartet Sampling – land plants

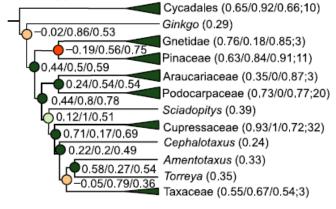


403.

#### C. Monocots

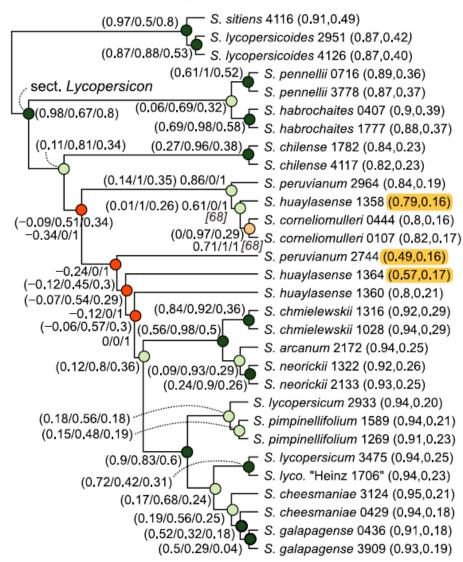


#### F. Acrogymnospermae



# Quartet Sampling – generic level

#### A. Solanum sect. Lycopersicon



Pease et al. (2016)



https://github.com/FePhyFoFum/quartetsampling

- requirements
  - Python 3.x (Numpy and Scipy for some options)
  - RAxML-ng 0.9.0 (or RAxML 8.1+, \*PAUP, IQ-TREE 1.6.x)
- NEWICK phylogeny
- alignment in Relaxed Phylip Format DNA or AA
- RAxML-style partitions file (optional)
- python3 quartet\_sampling.py -tree TREE.nwk -align ALIGNMENT.phy -reps 100 -threads 4 -lnlike 2



https://github.com/FePhyFoFum/quartetsampling

#### output tables

- RESULT.node.scores.csv (scores and other info per branch/terminal)
- RESULT.node.counts.csv (counts of concordant and discordant quartet arrangements)

#### output trees

- RESULT.labeled.tre.freq/qc/qd/qu (Newick tree with the each internal branch labeled with frequency of concordant replicates or QC/QD/QI scores)
- RESULT.labeled.tre.figtree (FigTree format phylogeny that contains all QS scores and a "score" field with QC/QD/QI for internal branches)

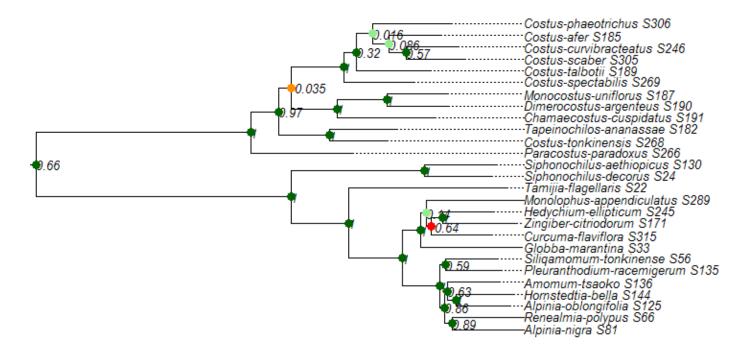


https://github.com/FePhyFoFum/quartetsampling

modify and plot tree using a custom script (bash/R)

https://github.com/tomas-fer/scripts/blob/master/quartetsampling.r

- RESULT.labeled.tre.qc tree with 'qc' values (used later for coloring nodes)
- RESULT.labeled.tre.figtree tree with all values (used for plotting the tree and three scores





https://github.com/FePhyFoFum/quartetsampling

- start interactive job on MetaCentrum
  - qsub -I -l select=1:ncpus=4:mem=4gb
- go to your directory (with species tree and concatenated alignment)
- download quartet sampling from GitHub
  - git clone https://github.com/FePhyFoFum/quartetsampling.git
- enable modules
  - module add python-3.6.2-gcc
  - module add raxml-ng-8
- run this to see options
  - python3 quartetsampling/pysrc/quartet\_sampling.py -h
- quartetsampling/pysrc/quartet\_sampling.py --tree Astral.tre -- align concatenated.phylip --reps 100 --threads 4 --lnlike 2
- process the tree with the instructions in

https://github.com/tomas-fer/scripts/blob/master/quartetsampling.r

## Gene selection/filtering

#### missing data

- bases per accession (...remove accession)
- species per gene (...remove gene)
- alignment improvement

#### variability/informativness

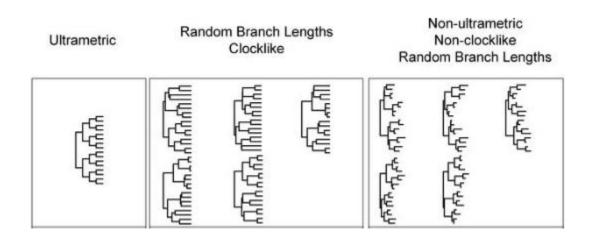
- information content
- nr. or % variable/parsimony informative sites
- GC content
- evolutionary rate (slow/fast genes)

#### tree characteristics

- overall bootstrap support (higher BS = stronger phylogenetic signal)
- **clocklikeness** (a measure how close to ultrametric a tree is: the algorithm finds a root that minimizes the coefficient of variation in root to tip distances and returns that value; a lower value is more clock-like, an ultrametric tree has a score of 0)
- long branch score (standard deviation from the taxon-specific long branch score defined by Struck, 2014)
- **Saturation** (simple linear regression on uncorrected p-distances against inferred distances, i.e., branch length slope and R<sup>2</sup>; higher values mean lower saturation potential)

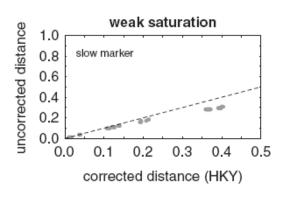
### Clocklikeness

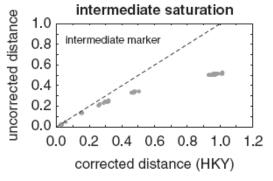
- a measure how close to ultrametric a tree is
- the algorithm finds a root that minimizes the coefficient of variation in root to tip distances and returns that value
- a lower value is more clock-like
- an ultrametric tree has a score of 0

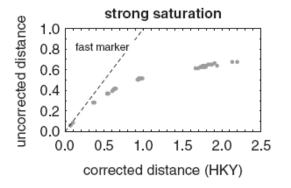


### Saturation

- simple linear regression on
  - uncorrected p-distances
  - inferred distances, i.e., branch length
- slope and R<sup>2</sup> is reported
- higher values mean lower saturation potential





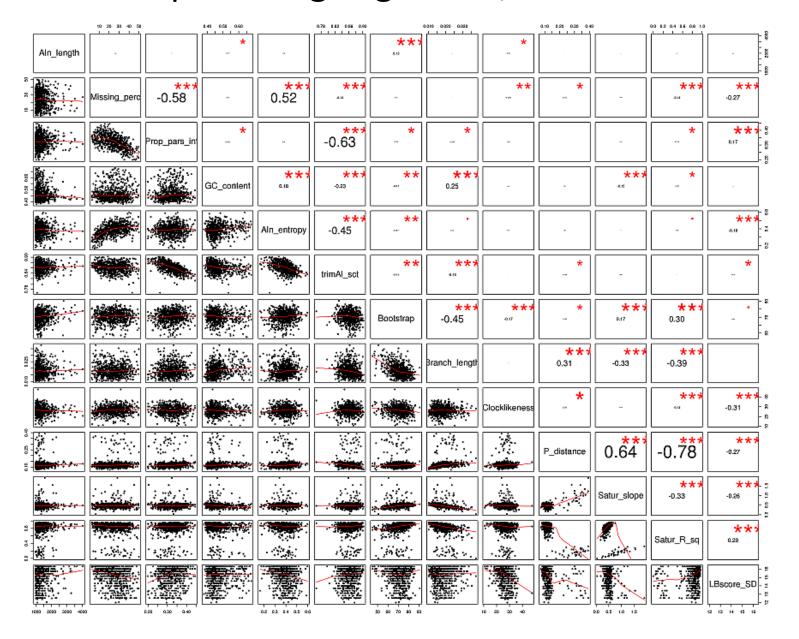


#### How to calculate alignment/tree characteristics?

- AMAS (<a href="https://github.com/marekborowiec/AMAS">https://github.com/marekborowiec/AMAS</a>)
  - concat, convert, summary, remove, translate
  - python3 AMAS.py summary -f fasta -d dna -i \*.fasta

- R scripts (e.g., https://github.com/marekborowiec/good\_genes)
  - average bootstrap
  - average branch length
  - saturation (slope, R<sup>2</sup>)

#### Relationships among alignment/tree characteristics



# Thank you...



dragon blood tree (*Dracaena cinnabari*), Socotra

#### References

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